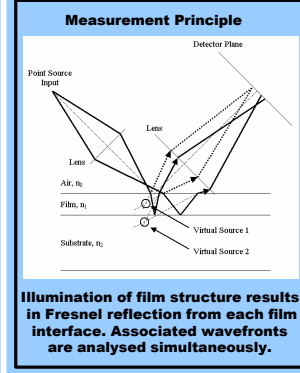


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Aberration Modelling



- Illumination of a thin film with a converging laser beam results in aberrations being introduced into reflected fields.
- The analysis of such aberrations allows a measure of film thickness and surface shape in a single measure.
- A thickness retrieval algorithm based on Moore – Penrose pseudo-inverse can be formulated to retrieve film thickness and surface tilt from aberration mode strengths.

Each aberration coefficient can be written as a combined linear function of thickness (d) and tilt (t):

$$s_m = a_m d + b_m t$$

By selecting various Zernike coefficients this can be expressed in matrix form:

$$\sum = Mu$$

where:

$$M = \begin{bmatrix} a_{m_1} & b_{m_1} \\ a_{m_2} & b_{m_2} \\ \vdots & \vdots \\ a_{m_n} & b_{m_n} \end{bmatrix}, \quad \sum = \begin{bmatrix} s_{m_1} \\ s_{m_2} \\ \vdots \\ s_{m_n} \end{bmatrix}, \quad u = \begin{bmatrix} d \\ t \end{bmatrix}$$

Thickness and tilt are then calculated using:

$$u = M^\dagger \sum$$

Example calculation: 100µm film, 1mrad tilt

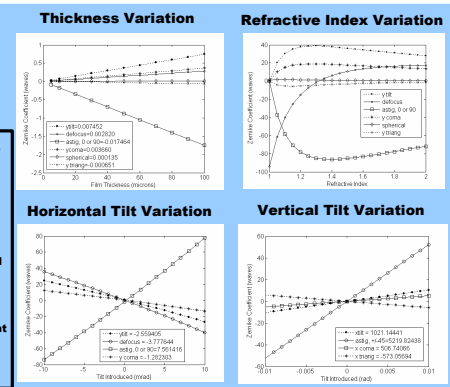
$$M = \begin{bmatrix} 0.007452 & -2.559405 \\ 0.002820 & -3.777644 \\ -0.017464 & 7.561416 \\ 0.003660 & -1.282303 \end{bmatrix}, \quad \sum = \begin{bmatrix} -1.8246472 \\ -3.512169 \\ 5.8394112 \\ -0.9215989 \end{bmatrix}$$

Values gained from gradients of straight line fits in plots.

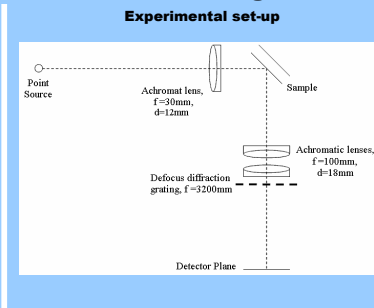
$$u = \begin{bmatrix} d \\ t \end{bmatrix} = M^\dagger \sum = \begin{bmatrix} 100.48 \\ 1.0045 \end{bmatrix}$$

Effect of Refractive Index.

- Aberration mode strength has dependency on refractive index.
- A non-linear relationship exists between mode strength and refractive index from plot.
- This non-linear relationship could be used to indicate a change in material refractive index.
- Refractive index has limited impact on thickness measurement when refractive index limited to 1.4 to 1.7.



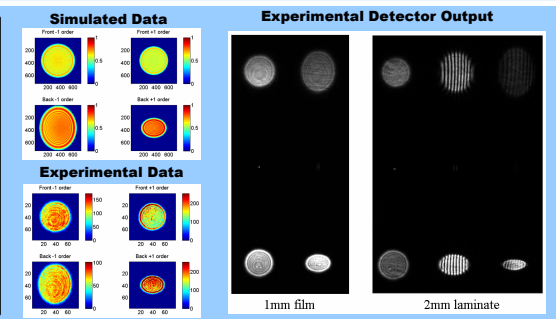
Wavefront sensing for thin film metrology



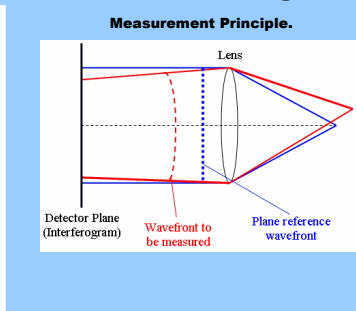
- Sample under test illuminated with focused laser beam with focus nominally set at the first film interface.
- Wavefront sensor consists of lens, grating and detector.
- Wavefront sensor analyses each Fresnel reflection from each film interface.
- Wavefront reconstruction allows measurement of film thickness and surface tilt to be made simultaneously (from analysis above).
- Measurement of interface profile possible.
- Distorted diffraction grating used to implement phase diversity wavefront sensing.
- Experimental results match simulated data.
- Measurements made on thick laminates (1-2mm).
- Accuracy of 50nm achieved to date.
- Dynamic range of instrument from 10µm to 8mm.

System Simulation

- System simulated using extended source analysis using Optalix ray tracing software package.
- Simulated data allowed size of diffraction order images to be calculated and used to develop thickness retrieval algorithm.
- Simulated data was compared with experimental results as shown with sizes differing by <1 pixel.
- Phase retrieval can be carried out on simulated data to reconstruct wavefront.
- Full wavefront analysis of simulated and experimental data will allow film thickness and interface profile to be measured simultaneously.



Film thickness using interference



- Reflected wavefronts from film under measurement produce interferogram.
- Retrieval of phase gives measure of wavefront difference, i.e. aberrations introduced by the film structure.
- Monitoring of such interferograms allows film thickness to be measured.
- Suitable for very thin films and laminates.

Reference wavefront can be expressed as:

$$a(x, y) = |a(x, y)| \exp[-j\ell(x, y)]$$

Wavefront to be measured can be expressed as:

$$A(x, y) = |A(x, y)| \exp[-j\gamma(x, y)]$$

The intensity at the detector plane is then expressed as a combination of both wavefronts:

$$I(x, y) = |A(x, y)|^2 + |a(x, y)|^2 + 2|A(x, y)||a(x, y)| \cos[\gamma(x, y) - \ell(x, y)]$$

Phase Unwrapping.

- The interferogram data must be interpreted to retrieve wrapped phase.
- Phase retrieved by use of FFT method to isolate sideband data and re-centring.
- Wrapped phase is then unwrapped using common techniques to identify dislocations in the wrapped phase.

Interferogram Data: (a) through (e)

Retrieved Unwrapped Phase: (a) through (e)

A Zernike fit is then carried out on the unwrapped phase to determine aberration mode strengths

A linear relationship exists between retrieved mode strengths and film thickness as shown. A measurement of film and laminate thickness possible using such methods.

For more information...